

# Package ‘iqLearn’

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**Description** Estimate an optimal dynamic treatment regime using Interactive Q-learning.

**License** GPL-2

**LazyData** TRUE

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bmiData	<i>Adolescent BMI data set (generated toy example)</i>
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## Description

This data set was generated to mimic data from a two-stage randomized clinical trial studying the effect of meal replacement shakes on adolescent obesity. It contains the following covariates collected at the start of the first stage: "gender," "race," "parent\_BMI," and "baseline\_BMI". At the second-stage, "month4\_BMI" was collected. Variables "A1" and "A2" are the randomized treatments at stage one and two, and "month12\_BMI" is the primary outcome collected at the end of stage two.

## Usage

```
bmiData
```

## Format

A matrix with rows corresponding to patients.

## Source

Generated by Kristin A. Linn in R

---

 IQ1

*IQ-learning: Recommend stage 1 treatment*


---

**Description**

Recommends the IQ-estimated optimal first-stage treatment for a patient with observed stage 1 variables.

**Usage**

```
IQ1(mainObj, cmObj, sigObj, dens, h1main, h1cm, h1sig)
```

**Arguments**

mainObj	object of type learnIQ1main
cmObj	object of type learnIQ1cm
sigObj	object of type learnIQ1var
dens	method of density estimation, either "norm" for normal location-scale density estimate or "nonpar" for the empirical density estimator
h1main	vector of observed first-stage main effects corresponding to the variables in H1Main used in learnIQ1main()
h1cm	vector of observed first-stage main effects corresponding to the variables in H1CMean used in learnIQ1cm()
h1sig	vector of observed first-stage main effects corresponding to the variables in H1CVar used in learnIQ1var()

**Details**

Use the estimated optimal first-stage decision rule from learnIQ1() to recommend the best stage 1 treatment for a patient presenting with history  $h_1$ . It is **essential** that  $h_1$ main include the **same variables and ordering** as H1Main. If a formula was used to fit learnIQ1main(), we recommend checking summary(<learnIQ1main object>) for the correct order of  $h_2$ . Similarly for  $h_1$ cm and  $h_1$ sig. dens can be chosen by looking at a normal QQ-plot of the standardized residuals from the contrast mean and variance modeling steps.

**Value**

q1Pos	estimated value of the first-stage Q-function when $H_1=h_1$ and $A_1=1$
q1Neg	estimated value of the first-stage Q-function when $H_1=h_1$ and $A_1=-1$
q1opt	estimated optimal first-stage treatment for a patient presenting with $h_1$

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

## References

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

## See Also

[learnIQ1main](#), [learnIQ1cm](#), [learnIQ1var](#),

## Examples

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
summary (fitIQ2)
## model conditional expected value of main effect term
fitIQ1main = learnIQ1main (~ gender + race + parent_BMI + baseline_BMI
  + A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitIQ2)
## model conditional mean of contrast function
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1", c
  ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
## variance modeling
fitIQ1var = learnIQ1var (~ gender + race + parent_BMI + baseline_BMI +
  A1*(parent_BMI), data=bmiData, "A1", c ("parent_BMI"), "hetero",
  fitIQ1cm)
## new patient
h1 = c (1, 1, 30, 35)
optIQ1 = IQ1 (fitIQ1main, fitIQ1cm, fitIQ1var, "nonpar", h1, h1, h1)
optIQ1$q1opt
```

---

 IQ2

*IQ-learning: Recommend stage 2 treatment*


---

**Description**

Recommends the estimated optimal second-stage treatment for a given stage 2 history,  $h_2$ .

**Usage**

```
IQ2(object, h2)
```

**Arguments**

object	object of type <code>learnIQ2</code>
h2	vector of observed second-stage main effects corresponding to the variables in H2 used in <code>learnIQ2()</code>

**Details**

Use the estimated optimal second-stage decision rule from `learnIQ2()` to recommend the best stage 2 treatment for a patient presenting with history  $h_2$ . It is **essential** that  $h_2$  include the **same variables and ordering** as H2. If a formula was used to fit `learnIQ2()`, we recommend checking `summary(<learnIQ2 object>)` for the correct order of  $h_2$ .

**Value**

q2Pos	estimated value of the second-stage Q-function when $H_2=h_2$ and $A_2=1$
q2Neg	estimated value of the second-stage Q-function when $H_2=h_2$ and $A_2=-1$
q2opt	estimated optimal second-stage treatment for a patient presenting with $h_2$

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", *Journal of Statistical Software*, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", *Biometrika*, 101(4), 831-847.

**See Also**

[learnIQ2](#), [summary.learnIQ2](#), [plot.learnIQ2](#)

**Examples**

```

## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
summary (fitIQ2)
## new patient
h2 = c (1, 30, 45)
optIQ2 = IQ2 (fitIQ2, h2)
optIQ2$q2opt

```

---

iqResids

*IQ-learning: standardized residuals*


---

**Description**

Creates an object containing the standardized residuals from the contrast mean and variance modeling steps.

**Usage**

```
iqResids(object)
```

**Arguments**

object                    object of type learnIQ1var

**Details**

Creates an object containing the standardized residuals from the contrast mean and variance modeling steps to be used with the plotting function `plot.iqResids`. The choice of density estimator in the next step of IQ-learning should be based on a QQ-plot of the standardized residuals.

**Value**

Returns `object$stdResids` from an object of type `learnIQ1var` in the form of an object of type `iqResids`.

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Laber, E.B., Linn, K.A., and Stefanski, L.A. (2013). Interactive Q-learning. *Submitted*.

**See Also**

[learnIQ1var](#), [plot.iqResids](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## model conditional mean of contrast function
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1", c
  ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
## variance modeling
fitIQ1var = learnIQ1var (~ gender + race + parent_BMI + baseline_BMI +
  A1*(parent_BMI), data=bmiData, "A1", c ("parent_BMI"), "hetero",
  fitIQ1cm)
## plot standardized residuals
fitResids = iqResids (fitIQ1var)
plot (fitResids)
```

---

`learnIQ1`*IQ-learning: estimate optimal first-stage rule*

---

**Description**

Estimates the optimal first-stage decision rule using IQ-learning.

**Usage**

```
learnIQ1(mainObj, cmObj, sigObj, dens)
```

**Arguments**

<code>mainObj</code>	object of type <code>learnIQ1main</code>
<code>cmObj</code>	object of type <code>learnIQ1cm</code>
<code>sigObj</code>	object of type <code>learnIQ1var</code>
<code>dens</code>	either "norm" or "nonpar"; density estimator to use for the conditional density of the contrast function

**Details**

If `dens="norm"` the normal location-scale density estimator is used, otherwise when `dens="nonpar"` the empirical density estimator is used.

**Value**

<code>optA1</code>	vector of estimated optimal first-stage treatment for the patients in the training data
--------------------	---

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", *Journal of Statistical Software*, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", *Biometrika*, 101(4), 831-847.

**See Also**

[learnIQ1main](#), [learnIQ1cm](#), [learnIQ1var](#)



**Examples**

```

## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
s2ints = c (2, 3)
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
    "month4_BMI"))
## model conditional expected value of main effect term
fitIQ1main = learnIQ1main (~ gender + race + parent_BMI + baseline_BMI
  + A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
    "parent_BMI"), fitIQ2)
## model conditional mean of contrast function
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1", c
  ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
## variance modeling
fitIQ1var = learnIQ1var (~ gender + race + parent_BMI + baseline_BMI +
  A1*(parent_BMI), data=bmiData, "A1", c ("parent_BMI"), "hetero",
  fitIQ1cm)
## get optimal first-stage txts
fitIQLearn = learnIQ1 (fitIQ1main, fitIQ1cm, fitIQ1var, "nonpar")

```

---

learnIQ1cm

*IQ-learning: contrast function mean regression*


---

**Description**

Estimates the mean of the contrast function by fitting a linear regression of the estimated contrast function term on first-stage history and treatment.

**Usage**

```
learnIQ1cm(object, ...)
```

```
## S3 method for class 'formula'
```

```
learnIQ1cm(formula, data, treatName, intNames, s2object, ...)
## Default S3 method:
learnIQ1cm(object, H1CMean, A1, s1cmInts, ...)
```

### Arguments

formula	formula for the contrast function mean regression
data	data frame containing variables used in formula
treatName	character string indicating the stage 1 treatment name
intNames	vector of characters indicating the names of the variables that interact with the stage 1 treatment in the contrast function mean regression model
s2object	object of type learnIQ2
object	object of type learnIQ2
H1CMean	matrix or data frame of first-stage covariates to include as main effects in the linear model
A1	vector of first-stage randomized treatments
s1cmInts	indices pointing to columns of H1CMean that should be included as treatment interaction effects in the linear model
...	other arguments to be passed to <code>lm()</code>

### Details

Fits a model of the form

$$E(H_{21}^T \beta_{21} | H_1, A_1) = H_{10}^T \beta_{10} + A_1 H_{11}^T \beta_{11},$$

where  $H_{10}$  and  $H_{11}$  are summaries of  $H_1$ . Though a slight abuse of notation, these summaries are not required to be the same as  $H_{10}$  and  $H_{11}$  in the main effect term regression or the variance model. For an object of type `learnIQ1cm`, `summary(object)` and `plot(object)` can be used for evaluating model fit.

### Value

betaHat10	estimated main effect coefficients; first is the intercept
betaHat11	estimated treatment interaction coefficients; first is the main effect of the first-stage treatment
s1cmFit	<code>lm()</code> object of the contrast mean regression fit
cmeanResids	residuals from the regression
cmPos	vector of predicted values with $A_1=1$ for all patients
cmNeg	vector of predicted values with $A_1=1$ for all patients
s1cmInts	indices of variables in H1CMean included as treatment interactions in the model; same as input <code>s1cmInts</code>
A1	vector of first-stage randomized treatments; same as input <code>A1</code>

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", *Journal of Statistical Software*, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", *Biometrika*, 101(4), 831-847.

**See Also**

[learnIQ2](#), [summary.learnIQ1cm](#), [plot.learnIQ1cm](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
s2ints = c (2, 3)
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1",
  c ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
summary (fitIQ1cm)
plot (fitIQ1cm)
```

---

learnIQ1main

*IQ-learning: main effect term regression*

---

**Description**

Fits a linear regression of the estimated main effect term on first-stage history and treatment.

**Usage**

```
learnIQ1main(object, ...)

## S3 method for class 'formula'
learnIQ1main(formula, data, treatName, intNames, s2object, ...)
## Default S3 method:
learnIQ1main(object, H1Main, A1, s1mainInts, ...)
```

**Arguments**

formula	formula for the main effect term regression
data	data frame containing variables used in formula
treatName	character string indicating the stage 1 treatment name
intNames	vector of characters indicating the names of the variables that interact with the stage 1 treatment in the main effect term regression model
s2object	object of type learnIQ2
object	object of type learnIQ2
H1Main	matrix or data frame of first-stage covariates to include as main effects in the linear model
A1	vector of first-stage randomized treatments
s1mainInts	indices pointing to columns of H1Main that should be included as treatment interaction effects in the linear model
...	other arguments to be passed to <code>lm()</code>

**Details**

Fits a model of the form

$$E(H_{20}^T \beta_{20} | H_1, A_1) = H_{10}^T \alpha_0 + A_1 H_{11}^T \alpha_1,$$

where  $H_{10}$  and  $H_{11}$  are summaries of  $H_1$ . For an object of type `learnIQ1main`, `summary(object)` and `plot(object)` can be used for evaluating model fit.

**Value**

alphaHat0	estimated main effect coefficients; first is the intercept
alphaHat1	estimated treatment interaction coefficients; first is the main effect of the first-stage treatment
s1MainFit	<code>lm()</code> object of the main effect term regression fit
mainPos	vector of predicted values with $A_1=1$ for all patients
mainNeg	vector of predicted values with $A_1=-1$ for all patients
s1mainInts	indices of variables in H1Main included as treatment interactions in the model; same as input <code>s1mainInts</code>
A1	vector of first-stage randomized treatments; same as input <code>A1</code>

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[learnIQ2](#), [summary.learnIQ1main](#), [plot.learnIQ1main](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
s2ints = c (2, 3)
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## model conditional expected value of main effect term
fitIQ1main = learnIQ1main (fitIQ2, s1vars, a1, c (1, 3))
fitIQ1main = learnIQ1main (~ gender + race + parent_BMI + baseline_BMI
  + A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitIQ2)

summary (fitIQ1main)
plot (fitIQ1main)
```

**Description**

Estimates the variance function of the contrast function by fitting a constant variance function or a log linear model to the residuals of the contrast mean fit.

**Usage**

```
learnIQ1var(object, ...)

## S3 method for class 'formula'
learnIQ1var(formula, data, treatName, intNames,
method, cmObject, ...)
## Default S3 method:
learnIQ1var(object, H1CVar, s1sInts, method, ...)
```

**Arguments**

formula	right-hand side formula containing the linear model to be used for the log-transformed, squared residuals from the contrast function mean fit
data	data frame containing variables used in formula
treatName	character string indicating the stage 1 treatment name
intNames	vector of characters indicating the names of the variables that interact with the stage 1 treatment in the contrast function variance model
method	either "homo" for a constant variance function or "hetero" for a log-linear variance function; default method is "homo"
cmObject	object of type learnIQ1cm
object	object of type learnIQ1cm
H1CVar	matrix or data frame of first-stage covariates to include as main effects in the log-linear model; default is NULL for a constant variance fit
s1sInts	indices pointing to columns of H1CVar that should be included as treatment interaction effects in the log-linear model; default is NULL
...	additional arguments to be passed to lm() when fitting the hetero log-linear model

**Details**

If method="homo", computes the variance of the residuals from the contrast function mean fit. If method="hetero", fits a model of the form

$$E(\log e^2 | H_1, A_1) = H_{10}^T \gamma_0 + A_1 H_{11}^T \gamma_1,$$

where  $H_{10}$  and  $H_{11}$  are summaries of  $H_1$ . Though a slight abuse of notation, these summaries are not required to be the same as  $H_{10}$  and  $H_{11}$  in the main effect term regression or the contrast mean fit. Also,  $e^2 = H_{21}^T \beta_{21} - E(H_{21}^T \beta_{21} | H_1, A_1)$ . For an object of type learnIQ1var, summary(object) and plot(object) can be used for evaluating model fit.

**Value**

stdDev	standard deviation of the residuals from the contrast function mean fit when method="homo", otherwise NULL
stdResids	standardized residuals of the contrast function after mean and variance modeling, using either method="homo" or "hetero"
gammaHat0	estimated regression coefficients from the log-linear model main effects when method="hetero", otherwise NULL
gammaHat1	estimated regression coefficients from the log-linear model interaction effects when method="hetero", otherwise NULL
s1VarFit	lm() object from the log-linear model when method="hetero", otherwise NULL
homo	logical variable indicating if method="homo" was used
sigPos	vector of predicted values when A1=1 for all patients
sigNeg	vector of predicted values when A1=-1 for all patients
s1sInts	indices of variables in H1CVar included as treatment interactions in the model; same as input s1sInts

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

- Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.
- Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[learnIQ1cm](#), [iqResids](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
```

```

y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## model conditional expected value of main effect term
fitIQ1main = learnIQ1main (~ gender + race + parent_BMI + baseline_BMI
  + A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitIQ2)
## model conditional mean of contrast function
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1", c
  ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
## variance modeling
fitIQ1var = learnIQ1var (fitIQ1cm) ## constant variance fit
fitIQ1var = learnIQ1var (fitIQ1cm, s1vars, c (3, 4), method="hetero")
## non-constant variance fit
fitIQ1var = learnIQ1var (~ gender + race + parent_BMI + baseline_BMI +
  A1*(parent_BMI), data=bmiData, "A1", c ("parent_BMI",
  "hetero", fitIQ1cm)
## non-constant variance fit using formula specification

```

---

learnIQ2

*IQ-learning: second-stage regression*


---

### Description

Fits a linear regression of the response on second-stage history and treatment to estimate the optimal second-stage decision rule.

### Usage

```

learnIQ2(H2, ...)

## S3 method for class 'formula'
learnIQ2(formula, data, treatName, intNames, ...)
## Default S3 method:
learnIQ2(H2, Y, A2, s2ints, ...)

```

### Arguments

formula	stage 2 regression formula
data	data frame containing variables used in formula
treatName	character string indicating the stage 2 treatment name
intNames	vector of characters indicating the names of the variables that interact with the stage 2 treatment in the regression model
H2	matrix or data frame of second-stage covariates to include as main effects in the linear model



Y	response vector
A2	vector of second-stage randomized treatments
s2ints	indices pointing to columns of H2 that should be included as treatment interaction effects in the linear model
...	other arguments to be passed to <code>lm()</code>

### Details

Fits a model of the form

$$E(Y|H_2, A_2) = H_{20}^T \beta_{20} + A_2 H_{21}^T \beta_{21},$$

where  $H_{20}$  and  $H_{21}$  are summaries of  $H_2$ . For an object of type `learnIQ2`, `summary(object)` and `plot(object)` can be used for evaluating model fit.

### Value

betaHat20	estimated main effect coefficients; first is the intercept
betaHat21	estimated treatment interaction coefficients; first is the main effect of the second-stage treatment
s2Fit	<code>lm()</code> object of the second-stage regression fit
optA2	vector of estimated optimal second-stage treatments for the patients in the training data
main	estimated main effect vector, $H_{20}^T \hat{\beta}_{20}$
contrast	estimated contrast function vector, $H_{21}^T \hat{\beta}_{21}$
s2ints	indices of variables in H2 included as treatment interactions in the model; same as input <code>s2ints</code>
A2	vector of second-stage randomized treatments; same as input <code>A2</code>

### Author(s)

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

### References

- Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", *Journal of Statistical Software*, 64(1), 1–25.
- Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", *Biometrika*, 101(4), 831-847.

### See Also

[summary.learnIQ2](#), [plot.learnIQ2](#)

**Examples**

```

## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
s2ints = c (2, 3)
## second-stage regression
fitIQ2 = learnIQ2 (s2vars, y, a2, s2ints)
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
    "month4_BMI"))

summary (fitIQ2)
plot (fitIQ2)

```

---

plot.iqResids

*Plot the standardized residuals*


---

**Description**

Plot the standardized residuals that arise from the contrast function mean and variance modeling.

**Usage**

```

## S3 method for class 'iqResids'
plot(x, ...)

```

**Arguments**

x	object of type iqResids
...	additional arguments to be passed to plot()

**Details**

Can be used to decide which density estimator ("norm" or "nonpar") should be used for the conditional density of the contrast function given first-stage history and treatment.

**Value**

Returns a normal QQ-plot of the standardized residuals.

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[iqResids](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
s2ints = c (2, 3)
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## model conditional mean of contrast function
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1",
  c ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
## variance modeling
fitIQ1var = learnIQ1var (~ gender + race + parent_BMI + baseline_BMI +
  A1*(parent_BMI), data=bmiData, "A1", c ("parent_BMI"), "hetero",
  fitIQ1cm)
## plot standardized residuals
fitResids = iqResids (fitIQ1var)
plot (fitResids)
```

---

plot.learnIQ1cm      *Residual plots for the contrast mean model*

---

### Description

Displays common residual plots that can be used to diagnose model fit for the contrast function mean model.

### Usage

```
## S3 method for class 'learnIQ1cm'  
plot(x, ...)
```

### Arguments

x                    object of type learnIQ1cm  
...                   additional arguments to be passed to plot()

### Value

None.

### Author(s)

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

### References

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

### See Also

[learnIQ1cm](#)

### Examples

```
## load in two-stage BMI data  
data(bmiData)  
bmiData$A1[which(bmiData$A1=="MR")] = 1  
bmiData$A1[which(bmiData$A1=="CD")] = -1  
bmiData$A2[which(bmiData$A2=="MR")] = 1  
bmiData$A2[which(bmiData$A2=="CD")] = -1  
bmiData$A1 = as.numeric(bmiData$A1)  
bmiData$A2 = as.numeric(bmiData$A2)  
s1vars = bmiData[,1:4]
```

```

s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
s2ints = c (2, 3)
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## model conditional mean of contrast function
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1", c
  ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
plot (fitIQ1cm)

```

---

plot.learnIQ1main      *Residual plots for the main effect term model*

---

## Description

Displays common residual plots that can be used to diagnose model fit for the main effect term regression.

## Usage

```

## S3 method for class 'learnIQ1main'
plot(x, ...)

```

## Arguments

x	object of type learnIQ1main
...	additional arguments to be passed to plot()

## Value

None.

## Author(s)

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

## References

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**[learnIQ1main](#)**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
s2ints = c (2, 3)
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## model conditional expected value of main effect term
fitIQ1main = learnIQ1main (fitIQ2, s1vars, a1, c (1, 3))
fitIQ1main = learnIQ1main (~ gender + race + parent_BMI + baseline_BMI
  + A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitIQ2)

plot (fitIQ1main)
```

---

plot.learnIQ1var

*Residual plots for the contrast variance model*


---

**Description**

Displays common residual plots that can be used to diagnose model fit for the contrast function variance model when method="hetero".

**Usage**

```
## S3 method for class 'learnIQ1var'
plot(x, ...)
```

**Arguments**

```
x          object of type learnIQ1var
...        additional arguments to be passed to plot()
```

**Details**

Will only plot residuals when method="hetero" was used to create the object of type learnIQ1var.

**Value**

None.

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[learnIQ1var](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1", c
  ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
fitIQ1var = learnIQ1var (~ gender + race + parent_BMI + baseline_BMI +
  A1*(parent_BMI), data=bmiData, "A1", c ("parent_BMI"), "hetero",
  fitIQ1cm)
plot (fitIQ1var)
```

---

`plot.learnIQ2`*Residual plots for the second-stage regression*

---

**Description**

Displays common residual plots that can be used to diagnose model fit for the second-stage regression model.

**Usage**

```
## S3 method for class 'learnIQ2'  
plot(x, ...)
```

**Arguments**

<code>x</code>	object of type <code>learnIQ2</code>
<code>...</code>	additional arguments to be passed to <code>plot()</code>

**Value**

None.

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[learnIQ2.default](#)

**Examples**

```
## load in two-stage BMI data  
data(bmiData)  
bmiData$A1[which(bmiData$A1=="MR")] = 1  
bmiData$A1[which(bmiData$A1=="CD")] = -1  
bmiData$A2[which(bmiData$A2=="MR")] = 1  
bmiData$A2[which(bmiData$A2=="CD")] = -1  
bmiData$A1 = as.numeric(bmiData$A1)  
bmiData$A2 = as.numeric(bmiData$A2)  
s1vars = bmiData[,1:4]
```



```

s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
plot (fitIQ2)

```

---

plot.qLearnS1

*Residual plots for the first-stage regression*


---

### Description

Displays common residual plots based on the model for the first-stage regression in Q-learning. Due to the response being a non-smooth, non-monotone transformation of the data, these plots may not be meaningful.

### Usage

```

## S3 method for class 'qLearnS1'
plot(x, ...)

```

### Arguments

x	object of type qLearnS1
...	additional arguments to be passed to plot()

### Value

None.

### Author(s)

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

### References

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

### See Also

[qLearnS1](#)

**Examples**

```

## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
## second-stage regression
fitQ2 = qLearnS2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## first-stage regression
fitQ1 = qLearnS1 (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitQ2)
plot (fitQ1)

```

---

plot.qLearnS2

*Residual plots for the second-stage regression*


---

**Description**

Displays common residual plots that can be used to diagnose model fit for the second-stage regression model.

**Usage**

```

## S3 method for class 'qLearnS2'
plot(x, ...)

```

**Arguments**

x                    object of type qLearnS2  
...                   other arguments to be passed to plot()

**Value**

None.

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[qLearnS2](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
## second-stage regression
fitQ2 = qLearnS2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
plot (fitQ2)
```

---

qLearnQ1

*Q-learning: Recommend stage 1 treatment*


---

**Description**

Recommends the Q-learning estimated optimal first-stage treatment for a given stage 1 history,  $h_1$ .

**Usage**

```
qLearnQ1(object, h1q)
```

**Arguments**

object	object of type qLearnS1
h1q	vector of observed first-stage main effects corresponding to the variables in H1q used in qLearnS1()

**Details**

Use the estimated optimal first-stage decision rule from qLearnS1() to recommend the best stage 1 treatment for a patient presenting with history h1q. It is **essential** that h1q include the **same variables and ordering** as H1q. If a formula was used to fit qLearnS1(), we recommend checking summary(<qLearnS1 object>) for the correct order of h1q.

**Value**

q1Pos	estimated value of the first-stage Q-function when $H1=h1$ and $A1=1$
q1Neg	estimated value of the first-stage Q-function when $H1=h1$ and $A1=-1$
q1opt	estimated optimal first-stage treatment for a patient presenting with $h1$

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

- Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.
- Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[qLearnS1](#), [summary.qLearnS1](#), [plot.qLearnS1](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
```

```

y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
## second-stage regression
fitQ2 = qLearnS2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## first-stage regression
fitQ1 = qLearnS1 (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitQ2)

summary (fitQ1)

h1q = c (1, 1, 35, 45);
optQ1 = qLearnQ1 (fitQ1, h1q);
optQ1$q1opt

```

---

qLearnQ2

*Q-learning: Recommend stage 2 treatment*


---

### Description

Recommends the estimated optimal second-stage treatment for a given stage 2 history,  $h2$ . This is the same as IQ2.

### Usage

```
qLearnQ2(object, h2)
```

### Arguments

object	object of type qLearnS2
h2	vector of observed second-stage main effects corresponding to the variables in H2 used in qLearnS2()

### Details

Use the estimated optimal second-stage decision rule from qLearnS2() to recommend the best stage 2 treatment for a patient presenting with history  $h2$ . It is **essential** that  $h2$  include the **same variables and ordering** as H2. If a formula was used to fit qLearnS2(), we recommend checking summary(qLearnS2) for the correct order of  $h2$ .

### Value

q2Pos	estimated value of the second-stage Q-function when $H2=h2$ and $A2=1$
q2Neg	estimated value of the second-stage Q-function when $H2=h2$ and $A2=-1$
q2opt	estimated optimal second-stage treatment for a patient presenting with $h2$

### Author(s)

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

## References

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

## See Also

[qLearnS2](#), [summary.qLearnS2](#), [plot.qLearnS2](#)

## Examples

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
fitQ2 = qLearnS2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
summary (fitQ2)

h2 = c (1, 30, 45)
optQ2 = qLearnQ2 (fitQ2, h2)
optQ2$q2opt
```

---

qLearnS1

*Q-learning: first-stage regression*

---

## Description

Regresses the predicted future outcome maximized over  $a_2$  on first-stage history and treatment to estimate the optimal first-stage decision rule using Q-learning.

**Usage**

```

qLearnS1(object, ...)

## S3 method for class 'formula'
qLearnS1(formula, data, treatName, intNames,
qS2object, ...)
## Default S3 method:
qLearnS1(object, H1q, A1, s1ints, ...)

```

**Arguments**

formula	right-hand sided stage 1 regression formula
data	data frame containing variables used in formula
treatName	character string indicating the stage 1 treatment name
intNames	vector of characters indicating the names of the variables that interact with the stage 1 treatment in the regression model
qS2object	object of type qLearnS2
object	object of type qLearnS2
H1q	matrix or data frame of first-stage covariates to include as main effects in the linear model
A1	vector of first-stage randomized treatments
s1ints	indices pointing to columns of H1q that should be included as treatment interaction effects in the linear model
...	other arguments to be passed to lm()

**Details**

Fits a model of the form

$$E(\tilde{Y}|H_1, A_1) = H_{10}^T \beta_{10} + A_1 H_{11}^T \beta_{11},$$

where  $H_{10}$  and  $H_{11}$  are summaries of  $H_1$ . For an object of type qLearnS1, `summary(object)` and `plot(object)` can be used for evaluating model fit.

**Value**

betaHat10	estimated main effect coefficients, beginning with the intercept
betaHat11	estimated treatment interaction coefficients, beginning with the main effect of treatment
optA1	vector of estimated optimal first-stage treatments for the patients in the training data
s1Fit	lm() object of the first-stage regression fit
s1ints	indices of variables in H1q included as treatment interactions in the model; same as input s1ints

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[summary.qLearnS2](#), [plot.qLearnS2](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
s2ints = c (2, 3)
## second-stage regression
fitQ2 = qLearnS2 (s2vars, y, a2, s2ints)
fitQ2 = qLearnS2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## first-stage regression
fitQ1 = qLearnS1 (fitQ2, s1vars, a1, c(3,4))
fitQ1 = qLearnS1 (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitQ2)
```

---

qLearnS2

*Q-learning: second-stage regression*

---

**Description**

Same as learnIQ2. Estimates the optimal second-stage decision rule using a linear regression of the response on second-stage history and treatment.



**Usage**

```

qLearnS2(H2, ...)

## S3 method for class 'formula'
qLearnS2(formula, data, treatName, intNames, ...)
## Default S3 method:
qLearnS2(H2, Y, A2, s2ints, ...)

```

**Arguments**

formula	stage 2 regression formula
data	data frame containing variables used in formula
treatName	character string indicating the stage 2 treatment name
intNames	vector of characters indicating the names of the variables that interact with the stage 2 treatment in the regression model
H2	matrix or data frame of second-stage covariates to include as main effects in the linear model
Y	response vector
A2	vector of second-stage randomized treatments
s2ints	indices pointing to columns of H2 that should be included as treatment interaction effects in the linear model
...	other arguments to be passed to <code>lm()</code>

**Details**

Fits a model of the form

$$E(Y|H_2, A_2) = H_{20}^T \beta_{20} + A_2 H_{21}^T \beta_{21},$$

where  $H_{20}$  and  $H_{21}$  are summaries of  $H_2$ . For an object of type `qLearnS2`, `summary(object)` and `plot(object)` can be used for evaluating model fit.

**Value**

betaHat20	estimated main effect coefficients; first is the intercept
betaHat21	estimated treatment interaction coefficients; first is the main effect of the second-stage treatment
Ytilde	Q2 function maximized over treatment $a_2$ ; the predicted future outcome assuming optimal treatment is given at the second stage to be used in the next step of the Q-learning algorithm
optA2	vector of estimated optimal second-stage treatments for the patients in the training data
s2Fit	<code>lm()</code> object of the second-stage regression fit
s2ints	indices of variables in H2 included as treatment interactions in the model; same as input <code>s2ints</code>

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[summary.qLearnS2](#), [plot.qLearnS2](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
s2ints = c (2, 3)
## second-stage regression
fitQ2 = qLearnS2 (s2vars, y, a2, s2ints)
fitQ2 = qLearnS2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))

summary (fitQ2)
plot (fitQ2)
```

---

summary.learnIQ1cm      *IQ-learning: contrast mean regression summary*

---

**Description**

Output from the contrast function mean regression in IQ-learning.

**Usage**

```
## S3 method for class 'learnIQ1cm'
summary(object, ...)
```

**Arguments**

```
object      object of type learnIQ1cm
...         additional arguments to be passed to summary()
```

**Details**

Regression output and other summary statistics from the contrast function mean regression. See `summary.lm` for more details.

**Value**

Computes and returns multiple summary statistics from the linear model in `object`. See `summary.lm` for a list of available summary statistics.

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", *Journal of Statistical Software*, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", *Biometrika*, 101(4), 831-847.

**See Also**

[learnIQ1cm](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
```

```

y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1", c
  ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)

summary (fitIQ1cm)

```

---

summary.learnIQ1main *IQ-learning: main effect regression summary*

---

## Description

Output from the main effect term regression in IQ-learning.

## Usage

```

## S3 method for class 'learnIQ1main'
summary(object, ...)

```

## Arguments

object	object of type learnIQ1main
...	additional arguments to be passed to summary()

## Details

Regression output and other summary statistics from the main effect term regression. See `summary.lm` for more details.

## Value

Computes and returns multiple summary statistics from the linear model in `object`. See `summary.lm` for a list of available summary statistics.

## Author(s)

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

## References

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", *Journal of Statistical Software*, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", *Biometrika*, 101(4), 831-847.

**See Also**[learnIQ1main](#)**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
fitIQ1main = learnIQ1main (~ gender + race + parent_BMI + baseline_BMI
  + A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitIQ2)
summary (fitIQ1main)
```

---

summary.learnIQ1var     *IQ-learning: contrast variance modeling summary*

---

**Description**

Output from the contrast function variance modeling in IQ-learning.

**Usage**

```
## S3 method for class 'learnIQ1var'
summary(object, ...)
```

**Arguments**

object	object of type learnIQ1var
...	additional arguments to be passed to summary()

**Details**

When method="homo" returns the standard deviation from the constant fit. When method="hetero" returns regression output and other summary statistics from the contrast function log-linear variance model. See `summary.lm` for more details.

**Value**

When method="hetero" computes and returns multiple summary statistics from the log-linear model in object. See `summary.lm` for a list of available summary statistics. Otherwise, when method="homo" returns only the standard deviation from the constant variance fit.

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

- Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", *Journal of Statistical Software*, 64(1), 1–25.
- Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", *Biometrika*, 101(4), 831-847.

**See Also**

[learnIQ1var](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1", c
  ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
fitIQ1var = learnIQ1var (fitIQ1cm)
summary (fitIQ1var)

fitIQ1var = learnIQ1var (~ gender + race + parent_BMI + baseline_BMI +
  A1*(parent_BMI), data=bmiData, "A1", c ("parent_BMI"), "hetero",
  fitIQ1cm)
summary (fitIQ1var)
```

---

summary.learnIQ2      *IQ-learning: second-stage regression summary*

---

## Description

Output from the second-stage regression in IQ-learning.

## Usage

```
## S3 method for class 'learnIQ2'  
summary(object, ...)
```

## Arguments

object            object of type learnIQ2  
...                additional arguments to be passed to summary()

## Details

Regression output and other summary statistics from the second-stage regression. See `summary.lm` for more details.

## Value

Computes and returns multiple summary statistics from the linear model in `object`. See `summary.lm` for a list of available summary statistics.

## Author(s)

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

## References

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", *Journal of Statistical Software*, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", *Biometrika*, 101(4), 831-847.

## See Also

[learnIQ2](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
summary (fitIQ2)
```

---

summary.qLearnS1

*Q-learning: first-stage regression summary*


---

**Description**

Output from the first-stage regression in Q-learning.

**Usage**

```
## S3 method for class 'qLearnS1'
summary(object, ...)
```

**Arguments**

object	object of type qLearnS1
...	additional arguments to be passed to summary()

**Details**

Regression output and other summary statistics from the second-stage regression. See `summary.lm` for more details.

**Value**

Computes and returns multiple summary statistics from the linear model in `object`. See `summary.lm` for a list of available summary statistics.



**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[qLearnS1](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
## second-stage regression
fitQ2 = qLearnS2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## first-stage regression
fitQ1 = qLearnS1 (fitQ2, s1vars, a1, c(3,4))
fitQ1 = qLearnS1 (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitQ2)

summary (fitQ1)
```

---

summary.qLearnS2

*Q-learning: second-stage regression summary*

---

**Description**

Output from the second-stage regression in Q-learning.

**Usage**

```
## S3 method for class 'qLearnS2'
summary(object, ...)
```

**Arguments**

```
object          object of type qLearnS2
...             additional arguments to be passed to summary()
```

**Details**

Regression output and other summary statistics from the second-stage regression. See `summary.lm` for more details.

**Value**

Computes and returns multiple summary statistics from the linear model in `object`. See `summary.lm` for a list of available summary statistics.

**Author(s)**

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

**References**

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", *Journal of Statistical Software*, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", *Biometrika*, 101(4), 831-847.

**See Also**

[qLearnS2](#)

**Examples**

```
## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
```

```

y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
fitQ2 = qLearnS2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
summary (fitQ2)

```

---

summary.value	<i>Estimate plug-in value</i>
---------------	-------------------------------

---

## Description

Output plug-in value estimates of treatment regimes based on the estimated IQ-learning parameters.

## Usage

```

## S3 method for class 'value'
summary(object, ...)

```

## Arguments

object	object of type value
...	other arguments to be passed to summary()

## Details

Can be used to print out the estimated plug-in values of non-dynamic regimes and any proposed regime, possibly estimated from IQ- or Q-learning.

## Value

None.

## Author(s)

Kristin A. Linn <kalinn@ncsu.edu>, Eric B. Laber, Leonard A. Stefanski

## References

Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.

Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

## See Also

[learnIQ2](#), [learnIQ1](#)

**Examples**

```

## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## model conditional expected value of main effect term
fitIQ1main = learnIQ1main (~ gender + race + parent_BMI + baseline_BMI
  + A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitIQ2)
## model conditional mean of contrast function
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1", c
  ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
## variance modeling
fitIQ1var = learnIQ1var (~ gender + race + parent_BMI + baseline_BMI +
  A1*(parent_BMI), data=bmiData, "A1", c ("parent_BMI"), "hetero",
  fitIQ1cm)
## get optimal first-stage txts
fitIQLearn = learnIQ1 (fitIQ1main, fitIQ1cm, fitIQ1var, "nonpar")
estVal = value (fitIQLearn$optA1, fitIQ2$optA2, y, a1, a2)
summary (estVal)

```

---

value

*Estimate plug-in value*


---

**Description**

Estimate the plug-in value of the any fixed treatment regime.

**Usage**

```
value(d1, d2, Y, A1, A2)
```

**Arguments**

d1	vector of first-stage treatments corresponding to the first-stage decision rule of the proposed regime
d2	vector of second-stage treatments corresponding to the second-stage decision rule of the proposed regime
Y	vector of responses
A1	vector of first-stage randomized treatments
A2	vector of second-stage randomized treatments

**Details**

The formula for the plug-in value estimate is

$$\frac{\sum_i Y_i * ind1_i * ind1_i}{\sum_i ind1_i * ind2_i}$$

where *ind1* and *ind2* are indicators that the first- and second-stage randomized treatments were consistent with the regime of interest.

**Value**

value	estimated plug-in value of the regime
valPosPos	estimated plug-in value of the regime that treats all patients with $A1=1$ and $A2 = 1$
valPosNeg	estimated plug-in value of the regime that treats all patients with $A1=1$ and $A2 = -1$
valNegPos	estimated plug-in value of the regime that treats all patients with $A1=-1$ and $A2=1$
valNegNeg	estimated plug-in value of the regime that treats all patients with $A1=-1$ and $A2=-1$

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**References**

- Linn, K. A., Laber, E. B., Stefanski, L. A. (2015) "iqLearn: Interactive Q-Learning in R", Journal of Statistical Software, 64(1), 1–25.
- Laber, E. B., Linn, K. A., and Stefanski, L. A. (2014) "Interactive model building for Q-learning", Biometrika, 101(4), 831-847.

**See Also**

[summary.value](#)

**Examples**

```

## load in two-stage BMI data
data (bmiData)
bmiData$A1[which (bmiData$A1=="MR")] = 1
bmiData$A1[which (bmiData$A1=="CD")] = -1
bmiData$A2[which (bmiData$A2=="MR")] = 1
bmiData$A2[which (bmiData$A2=="CD")] = -1
bmiData$A1 = as.numeric (bmiData$A1)
bmiData$A2 = as.numeric (bmiData$A2)
s1vars = bmiData[,1:4]
s2vars = bmiData[,c (1, 3, 5)]
a1 = bmiData[,7]
a2 = bmiData[,8]
## define response y to be the negative 12 month change in BMI from
## baseline
y = -(bmiData[,6] - bmiData[,4])/bmiData[,4]
## second-stage regression
fitIQ2 = learnIQ2 (y ~ gender + parent_BMI + month4_BMI +
  A2*(parent_BMI + month4_BMI), data=bmiData, "A2", c("parent_BMI",
  "month4_BMI"))
## model conditional expected value of main effect term
fitIQ1main = learnIQ1main (~ gender + race + parent_BMI + baseline_BMI
  + A1*(gender + parent_BMI), data=bmiData, "A1", c ("gender",
  "parent_BMI"), fitIQ2)
## model conditional mean of contrast function
fitIQ1cm = learnIQ1cm (~ gender + race + parent_BMI + baseline_BMI +
  A1*(gender + parent_BMI + baseline_BMI), data=bmiData, "A1", c
  ("gender", "parent_BMI", "baseline_BMI"), fitIQ2)
## variance modeling
fitIQ1var = learnIQ1var (~ gender + race + parent_BMI + baseline_BMI +
  A1*(parent_BMI), data=bmiData, "A1", c ("parent_BMI"), "hetero",
  fitIQ1cm)
## get optimal first-stage txts
fitIQLearn = learnIQ1 (fitIQ1main, fitIQ1cm, fitIQ1var, "nonpar")
estVal = value (fitIQLearn$optA1, fitIQ2$optA2, y, a1, a2)
estVal

```

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