

Package ‘gk’

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Description Functions for the g-and-k and generalised g-and-h distributions.

License GPL-2

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Suggests testthat

ByteCompile true

URL <https://github.com/dennisprangle/gk>

BugReports <https://github.com/dennisprangle/gk/issues>

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abc *Approximate Bayesian computation inference*

Description

Approximate Bayesian computation (ABC) inference for the g-and-k or g-and-h distribution.

Usage

```
abc(x, N, model = c("gk", "gh"), logB = FALSE, rprior, M,
    sumstats = c("all order statistics", "octiles", "moment estimates"),
    silent = FALSE)
```

Arguments

x	Vector of observations.
N	Number of iterations to perform.
model	Whether to fit g-and-k or g-and-h model.
logB	When true, the second parameter is log(B) rather than B.
rprior	A function with single argument, n, which returns a matrix with n rows consisting of samples from the prior distribution for 4 parameters e.g. (A,B,g,k).
M	Number of simulations to accept.
sumstats	Which summary statistics to use.
silent	When FALSE (the default) a progress bar is shown.

Details

This function performs approximate Bayesian inference for iid data from a g-and-k or g-and-h distribution, avoiding expensive density calculations. The algorithm samples many parameter vectors from the prior and simulates corresponding data from the model. The parameters are accepted or rejected based on how similar the simulations are to the observed data. Similarity is measured using weighted Euclidean distance between summary vectors of the simulations and observations. Several summaries can be used, including the complete order statistics or summaries based on octiles. In the latter case only the corresponding order statistics are simulated, speeding up the method.

Value

Matrix whose rows are accepted parameter estimates plus a column giving the ABC distances.

References

D. Prangle. gk: An R package for the g-and-k and generalised g-and-h distributions, 2017.

Examples

```

set.seed(1)
x = rgk(10, A=3, B=1, g=2, k=0.5) ##An unusually small dataset for fast execution of this example
rprior = function(n) { matrix(runif(4*n,0,10), ncol=4) }
abc(x, N=1E4, rprior=rprior, M=100)

```

abc_batch

Single batch of ABC

Description

Internal function carrying out part of ABC inference calculations

Usage

```
abc_batch(sobs, priorSims, simStats, M, v = NULL)
```

Arguments

sobs	Vector of observed summary statistics.
priorSims	Matrix whose rows are vector of parameters drawn from the prior.
simStats	Function mapping a vector of parameters to summary statistics.
M	How many simulations to accept in this batch.
v	Optional vector of estimated variances for each summary statistic

Details

Outputs a list containing: 1) matrix whose rows are accepted parameter vectors, and a column of resulting distances 2) value of v. If v is not supplied then variances are estimated here and returned. (The idea is that this is done for the first batch, and these values are reused from then on.)

dgh

g-and-h distribution functions

Description

Density, distribution function, quantile function and random generation for the generalised g-and-h distribution

Usage

```
dgh(x, A, B, g, h, c = 0.8, log = FALSE)
```

```
pgh(q, A, B, g, h, c = 0.8, zscale = FALSE)
```

```
qgh(p, A, B, g, h, c = 0.8)
```

```
rgh(n, A, B, g, h, c = 0.8)
```

Arguments

x	Vector of quantiles.
A	Vector of A (location) parameters.
B	Vector of B (scale) parameters. Must be positive.
g	Vector of g parameters.
h	Vector of h parameters. Must be non-negative.
c	Vector of c parameters. Often fixed at 0.8 which is the default.
log	If true the log density is returned.
q	Vector of quantiles.
zscale	If true the N(0,1) quantile of the cdf is returned.
p	Vector of probabilities.
n	Number of draws to make.

Details

The (generalised) g-and-h distribution is defined by its quantile function:

$$x(p) = A + B[1 + c \tanh(gz/2)]z \exp(hz^2/2),$$

where z is the standard normal quantile of p . Parameter restrictions include $B > 0$ and $h \geq 0$. Typically $c=0.8$. For more background information see the references.

`rgh` and `qgh` use quick direct calculations. However `dgh` and `pgh` involve slower numerical inversion of the quantile function.

Especially extreme values of the inputs will produce `pgh` output rounded to 0 or 1 (-Inf or Inf for `zscale=TRUE`). The corresponding `dgh` output will be 0 or -Inf for `log=TRUE`.

Value

`dgh` gives the density, `pgh` gives the distribution, `qgh` gives the quantile function, and `rgh` generates random deviates

References

Haynes 'Flexible distributions and statistical models in ranking and selection procedures, with applications' PhD Thesis QUT (1998) Rayner and MacGillivray 'Numerical maximum likelihood estimation for the g-and-k and generalized g-and-h distributions' *Statistics and Computing*, 12, 57-75 (2002)

Examples

```

p = 1:9/10 ##Some probabilities
x = qgh(seq(0.1,0.9,0.1), A=3, B=1, g=2, h=0.5) ##g-and-h quantiles
rgh(5, A=3, B=1, g=2, h=0.5) ##g-and-h draws
dgh(x, A=3, B=1, g=2, h=0.5) ##Densities of x under g-and-h
dgh(x, A=3, B=1, g=2, h=0.5, log=TRUE) ##Log densities of x under g-and-h
pgh(x, A=3, B=1, g=2, h=0.5) ##Distribution function of x under g-and-h

```

dgk *g-and-k distribution functions*

Description

Density, distribution function, quantile function and random generation for the g-and-k distribution.

Usage

```

dgk(x, A, B, g, k, c = 0.8, log = FALSE)

pgk(q, A, B, g, k, c = 0.8, zscale = FALSE)

qgk(p, A, B, g, k, c = 0.8)

rgk(n, A, B, g, k, c = 0.8)

```

Arguments

x	Vector of quantiles.
A	Vector of A (location) parameters.
B	Vector of B (scale) parameters. Must be positive.
g	Vector of g parameters.
k	Vector of k parameters. Must be at least -0.5.
c	Vector of c parameters. Often fixed at 0.8 which is the default.
log	If true the log density is returned.
q	Vector of quantiles.
zscale	If true the N(0,1) quantile of the cdf is returned.
p	Vector of probabilities.
n	Number of draws to make.

Details

The g-and-k distribution is defined by its quantile function:

$$x(p) = A + B[1 + c \tanh(gz/2)]z(1 + z^2)^k,$$

where z is the standard normal quantile of p . Parameter restrictions include $B > 0$ and $k \geq -0.5$. Typically $c=0.8$. For more background information see the references.

`rgk` and `qgk` use quick direct calculations. However `dgk` and `pgk` involve slower numerical inversion of the quantile function.

Especially extreme values of the inputs will produce `pgk` output rounded to 0 or 1 (`-Inf` or `Inf` for `zscale=TRUE`). The corresponding `dgk` output will be 0 or `-Inf` for `log=TRUE`.

Value

`dgk` gives the density, `pgk` gives the distribution, `qgk` gives the quantile function, and `rgk` generates random deviates

References

Haynes 'Flexible distributions and statistical models in ranking and selection procedures, with applications' PhD Thesis QUT (1998) Rayner and MacGillivray 'Numerical maximum likelihood estimation for the g-and-k and generalized g-and-h distributions' *Statistics and Computing*, 12, 57-75 (2002)

Examples

```
p = 1:9/10 ##Some probabilities
x = qgk(seq(0.1,0.9,0.1), A=3, B=1, g=2, k=0.5) ##g-and-k quantiles
rgk(5, A=3, B=1, g=2, k=0.5) ##g-and-k draws
dgk(x, A=3, B=1, g=2, k=0.5) ##Densities of x under g-and-k
dgk(x, A=3, B=1, g=2, k=0.5, log=TRUE) ##Log densities of x under g-and-k
pgk(x, A=3, B=1, g=2, k=0.5) ##Distribution function of x under g-and-k
```

fdsa

Finite difference stochastic approximation inference

Description

Finite difference stochastic approximation (FDSA) inference for the g-and-k or g-and-h distribution

Usage

```
fdsa(x, N, model = c("gk", "gh"), logB = FALSE, theta0, batch_size = 100,
alpha = 1, gamma = 0.49, a0 = 1, c0 = NULL, A = 100,
theta_min = c(-Inf, ifelse(logB, -Inf, 1e-05), -Inf, 0),
theta_max = c(Inf, Inf, Inf, Inf), silent = FALSE, plotEvery = 100)
```

Arguments

<code>x</code>	Vector of observations.
<code>N</code>	number of iterations to perform.
<code>model</code>	Whether to fit gk or gh model.
<code>logB</code>	When true, the second parameter is $\log(B)$ rather than B .
<code>theta0</code>	Vector of initial value for 4 parameters.
<code>batch_size</code>	Mini-batch size.
<code>alpha</code>	Gain decay for step size.
<code>gamma</code>	Gain decay for finite difference.
<code>a0</code>	Multiplicative step size tuning parameter (or vector of 4 values).
<code>c0</code>	Multiplicative finite difference step tuning parameter (or vector of 4 values).
<code>A</code>	Additive step size tuning parameter.
<code>theta_min</code>	Vector of minimum values for each parameter.
<code>theta_max</code>	Vector of maximum values for each parameter.
<code>silent</code>	When FALSE (the default) a progress bar and intermediate results plots are shown.
<code>plotEvery</code>	How often to plot the results if <code>silent==FALSE</code> .

Details

fdsa performs maximum likelihood inference for iid data from a g-and-k or g-and-h distribution, using simultaneous perturbation stochastic approximation. This should be faster than directly maximising the likelihood.

Value

Matrix whose rows are FDSA states: the initial state `theta0` and N subsequent states. The final row is the MLE estimate.

References

D. Prangle gk: An R package for the g-and-k and generalised g-and-h distributions, 2017.

Examples

```
set.seed(1)
x = rgk(10, A=3, B=1, g=2, k=0.5) ##An unusually small dataset for fast execution of this example
out = fdsa(x, N=100, theta0=c(mean(x),sd(x),0,0), theta_min=c(-5,1E-5,-5,0), theta_max=c(5,5,5,5))
```

fx *Exchange rate example*

Description

Performs a demo analysis of exchange rate data

Usage

```
fx(type = c("standard", "quick", "for paper"))
```

Arguments

type What type of demo to perform. standard runs the full demo displaying plots. quick is a fast demo suitable for testing the package. for paper saves pdfs which can be used in the paper.

Details

fx performs the analysis of exchange rate data in the supporting reference (Prangle 2017).

References

D. Prangle gk: An R package for the g-and-k and generalised g-and-h distributions, 2017.

Examples

```
## Not run:  
fx()  
  
## End(Not run)
```

improper_uniform_log_density
Improper uniform log density

Description

Returns log density of an improper prior for the g-and-k or g-and-h distribution

Usage

```
improper_uniform_log_density(theta)
```

Arguments

theta A vector of 4 parameters representing (A,B,g,k) or (A,B,g,h)

Details

`improper_uniform_log_density` takes a 4 parameter vector as input and returns a log density value. The output corresponds to an improper uniform with constraints that the second and fourth parameters should be non-negative. These ensure that the resulting parameters are valid to use in the g-and-k or g-and-h distribution is valid. This function is supplied as a convenient default prior to use in the `mcmc` function.

Value

Value of an (unnormalised) log density

Examples

```
improper_uniform_log_density(c(0,1,0,0)) ##Valid parameters - returns 0
improper_uniform_log_density(c(0,-1,0,0)) ##Invalid parameters - returns -Inf
```

<code>isValid</code>	<i>Check validity of g-and-k or g-and-h parameters</i>
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Description

Check whether parameter choices produce a valid g-and-k or g-and-h distribution.

Usage

```
isValid(g, k_or_h, c = 0.8, model = c("gk", "gh"), initial_z = seq(-1, 1,
  0.2))
```

Arguments

<code>g</code>	Vector of g parameters.
<code>k_or_h</code>	Vector of k or h parameters.
<code>c</code>	Vector of c parameters.
<code>model</code>	Whether to check the g-and-k or g-and-h model.
<code>initial_z</code>	Vector of initial z values to use in each optimisation.

Details

This function tests whether parameter choices provide a valid distribution. Only g k and c parameters need be supplied as A and B>0 have no effect. The function operates by numerically minimising the derivative of the quantile function, and returning TRUE if the minimum is positive. It is possible that a local minimum is found, so it is recommended to use multiple optimisation starting points, and to beware that false positive may still result!

Value

Logical vector denoting whether each parameter combination is valid.

References

D. Prangle and K. Peel. `gk`: An R package for the g-and-k and g-and-h distributions, in preparation.

Examples

```
isValid(0:10, -0.5)
isValid(0:10, 0.5, c=0.9, model="gh")
```

mcmc

Markov chain Monte Carlo inference

Description

Markov chain Monte Carlo (MCMC) inference for the g-and-k or g-and-h distribution

Usage

```
mcmc(x, N, model = c("gk", "gh"), logB = FALSE,
     get_log_prior = improper_uniform_log_density, theta0, Sigma0, t0 = 100,
     epsilon = 1e-06, silent = FALSE, plotEvery = 100)
```

Arguments

<code>x</code>	Vector of observations.
<code>N</code>	Number of MCMC steps to perform.
<code>model</code>	Whether to fit g-and-k or g-and-h model.
<code>logB</code>	When true, the second parameter is $\log(B)$ rather than B .
<code>get_log_prior</code>	A function with one argument (corresponding to a vector of 4 parameters e.g. A, B, g, k) returning the log prior density. This should ensure the parameters are valid - i.e. return $-\infty$ for invalid parameters - as the <code>mcmc</code> code will not check this.
<code>theta0</code>	Vector of initial value for 4 parameters.
<code>Sigma0</code>	MCMC proposal covariance matrix
<code>t0</code>	Tuning parameter (number of initial iterations without adaptation).
<code>epsilon</code>	Tuning parameter (weight given to identity matrix in covariance calculation).
<code>silent</code>	When FALSE (the default) a progress bar and intermediate results plots are shown.
<code>plotEvery</code>	How often to plot the results if <code>silent==FALSE</code> .

Details

`mcmc` performs Markov chain Monte Carlo inference for iid data from a g-and-k or g-and-h distribution, using the adaptive Metropolis algorithm of Haario et al (2001).

Value

Matrix whose rows are MCMC states: the initial state θ_0 and N subsequent states.

References

D. Prangle `gk`: An R package for the g-and-k and generalised g-and-h distributions, 2017. H. Haario, E. Saksman, and J. Tamminen. An adaptive Metropolis algorithm. *Bernoulli*, 2001.

Examples

```
set.seed(1)
x = rgk(10, A=3, B=1, g=2, k=0.5) ##An unusually small dataset for fast execution of this example
out = mcmc(x, N=1000, theta=c(mean(x),sd(x),0,0), Sigma=0.1*diag(4))
```

momentEstimates

Convert octiles to moment estimates

Description

Convert octiles to estimates of location, scale, skewness and kurtosis.

Usage

```
momentEstimates(octiles)
```

Arguments

`octiles` Vector of octiles.

Details

Converts octiles to robust estimate of location, scale, skewness and kurtosis as used by Drovandi and Pettitt (2011).

Value

Vector of moment estimates.

References

C. C. Drovandi and A. N. Pettitt. Likelihood-free Bayesian estimation of multivariate quantile distributions. *Computational Statistics & Data Analysis*, 2011.

orderstats	<i>Order statistics</i>
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Description

Sample a subset of order statistics of the Uniform(0,1) distribution

Usage

```
orderstats(n, orderstats)
```

Arguments

n	Total number of independent draws
orderstats	Which order statistics to generate, in increasing order

Details

Uniform order statistics are generated by the exponential spacings method (see Ripley for example).

Value

A vector of order statistics equal in length to orderstats

References

Brian Ripley 'Stochastic Simulation' Wiley (1987)

Examples

```
orderstats(100, c(25,50,75))
```

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